

# **Systematic errors from pixelization**

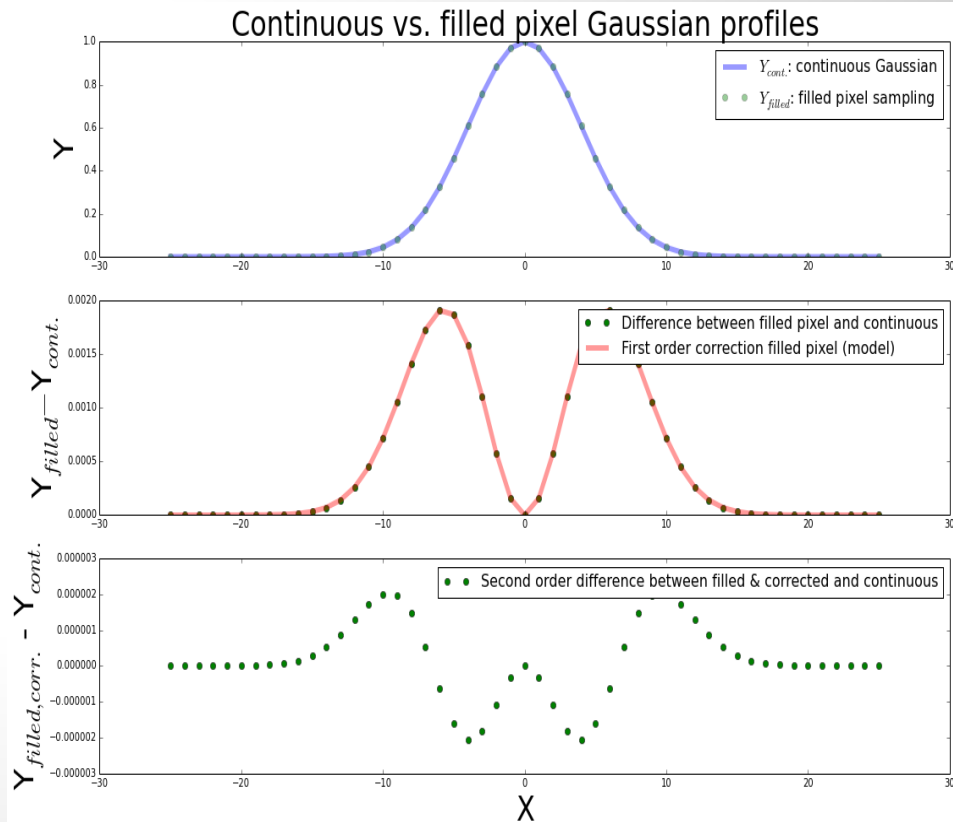
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# introduction

- Pixels of course, are not point-like detectors, but have characteristic width (among other properties)
- Incorrect model of pixel  $\rightarrow$  systematic error, large enough that it needs to be considered for precision cosmology

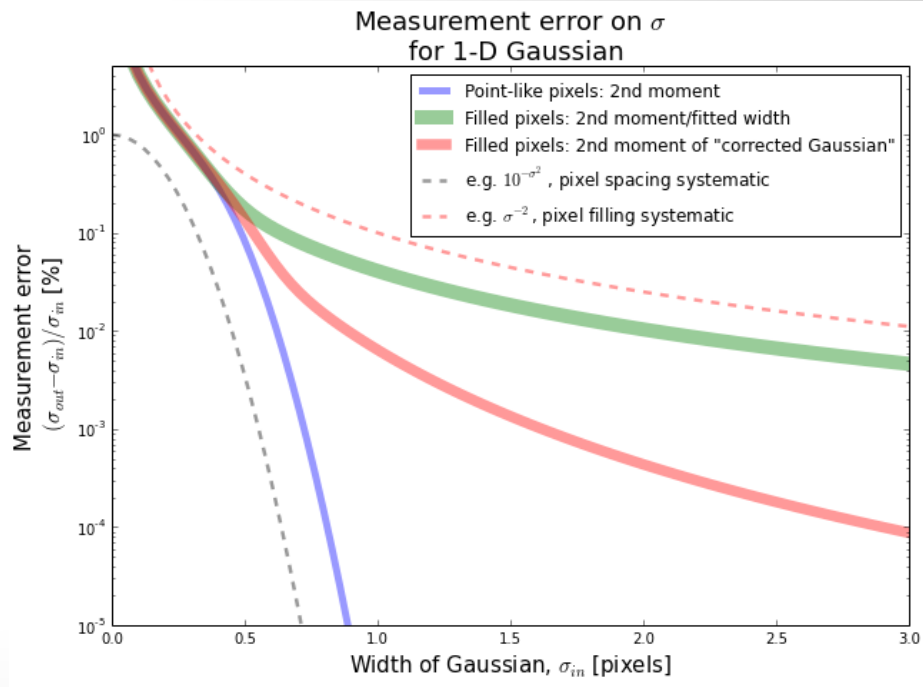
# simple example: size bias in fitting pixelized gaussian image

- Take continuous Gaussian  $g(x)$  and sample it at points  $x_i$  to get image  $i(x_i)$ 
  - small-scale information lost
  - point-like pix:  $i = \int g(x) * \delta(x - x_i)$
  - filled pix:  $i = \int g(x) * \text{rect}(x - x_i)$
- Difference between input continuous and “filled pixel” image is small but significant
  - can be modeled by integrating terms of Taylor series of Gaussian



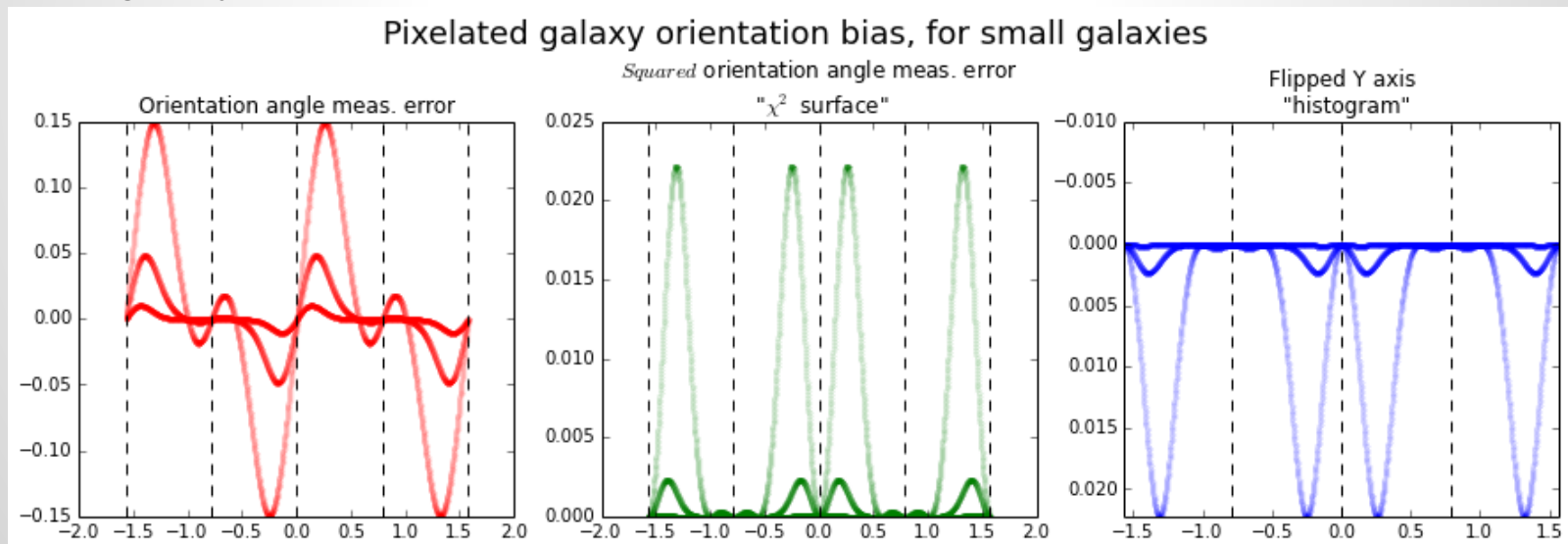
# simple example: continued

- Measuring the 2nd moment (or fitting a continuous Gaussian) to the pixelized image results in overestimate of width
  - Overestimates even if correction for pixelization “filling up” is taken into account
- Two types of errors here, 1) not accounting for “filling up” and 2) undersampling due to pixel spacing

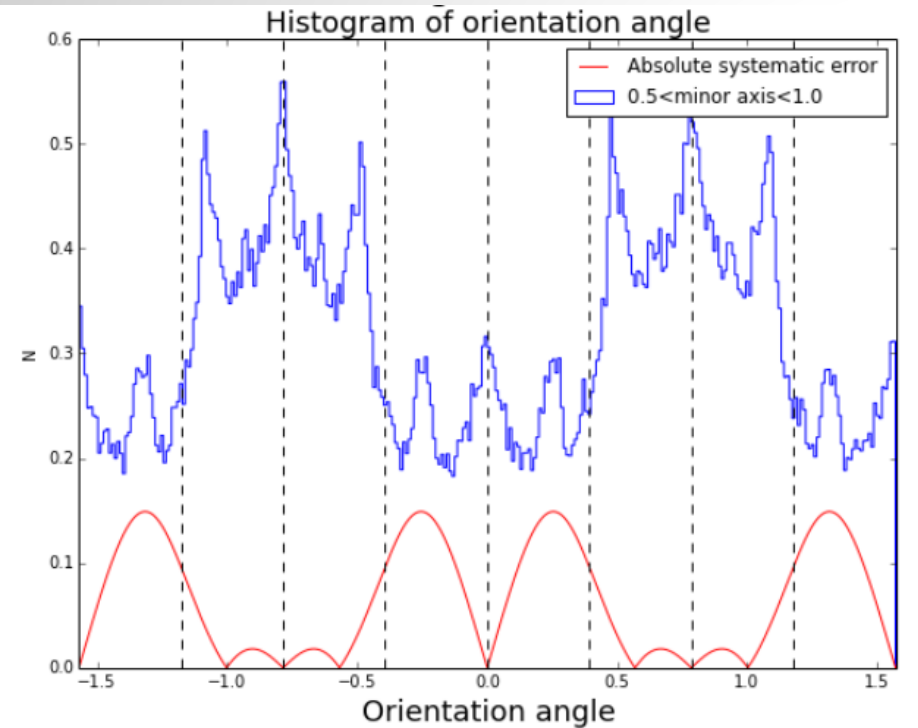


# size bias can lead to orientation bias in 2D

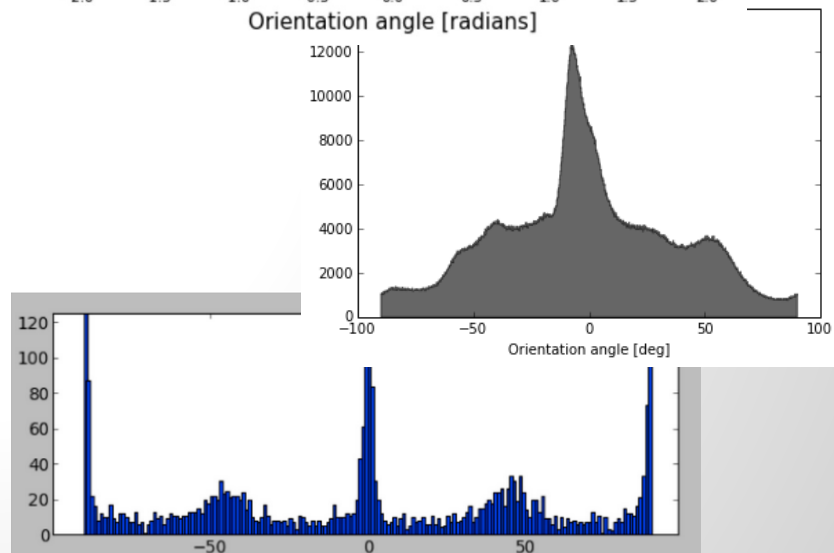
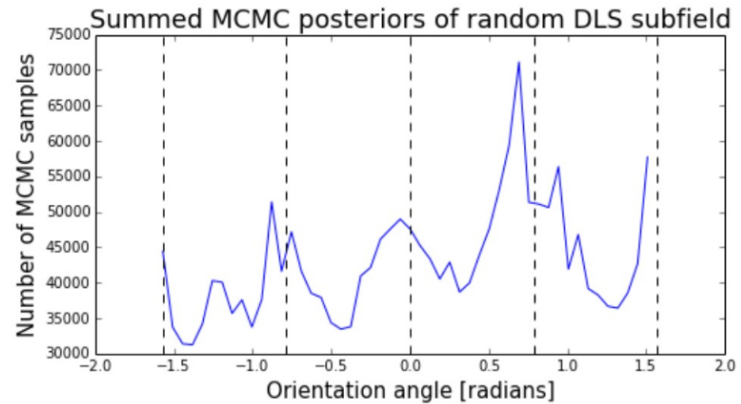
- As an elliptical Gaussian is rotated through the pixel plane, the X & Y 2nd moments change
- Changing input X&Y moments changes systematic error level
- Simple least-squares minimizer will find systematic error minima → orientation preference
- orientation bias is sourced from any size measurement bias



# evidence of orienta



...lots more



# need to model the pixel

not only must the pixel's width be taken into account, but other systematics too: ccd edge effects, astrometric residuals, charge spreading, backside bias of chip

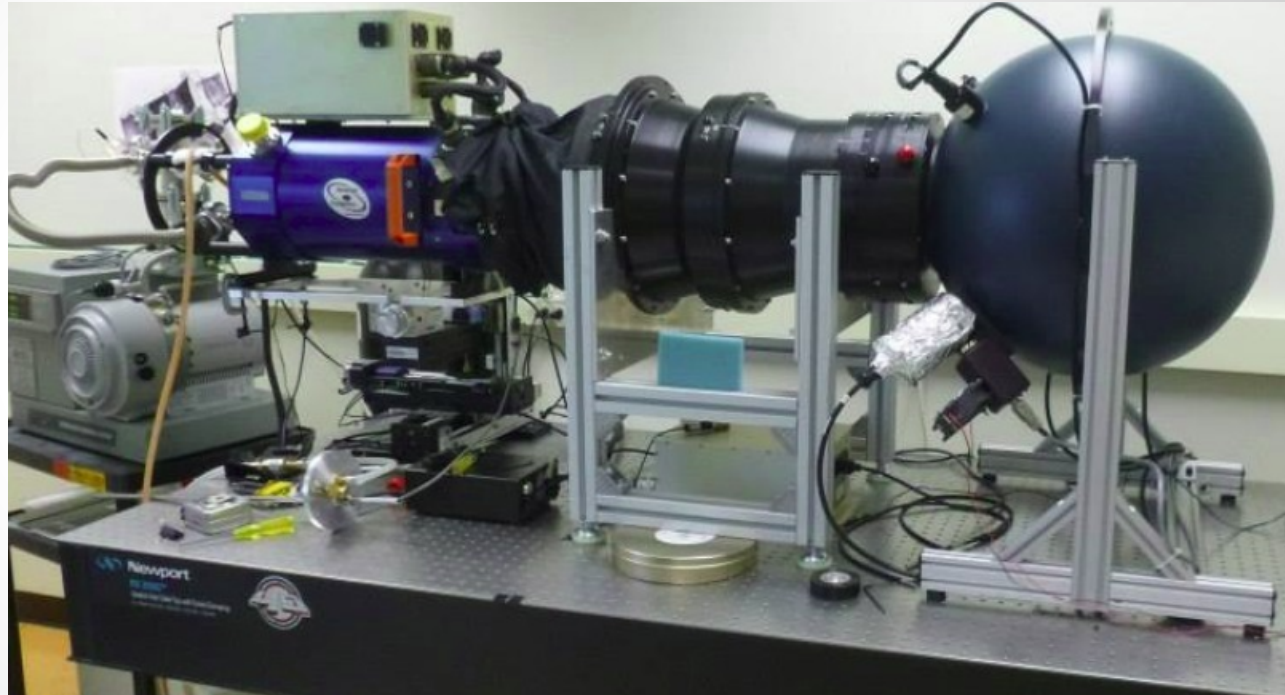
a full model of pixel is necessary for precision science, lots of work to do!

# facility for testing

f1.2 reimager with  
precision control over

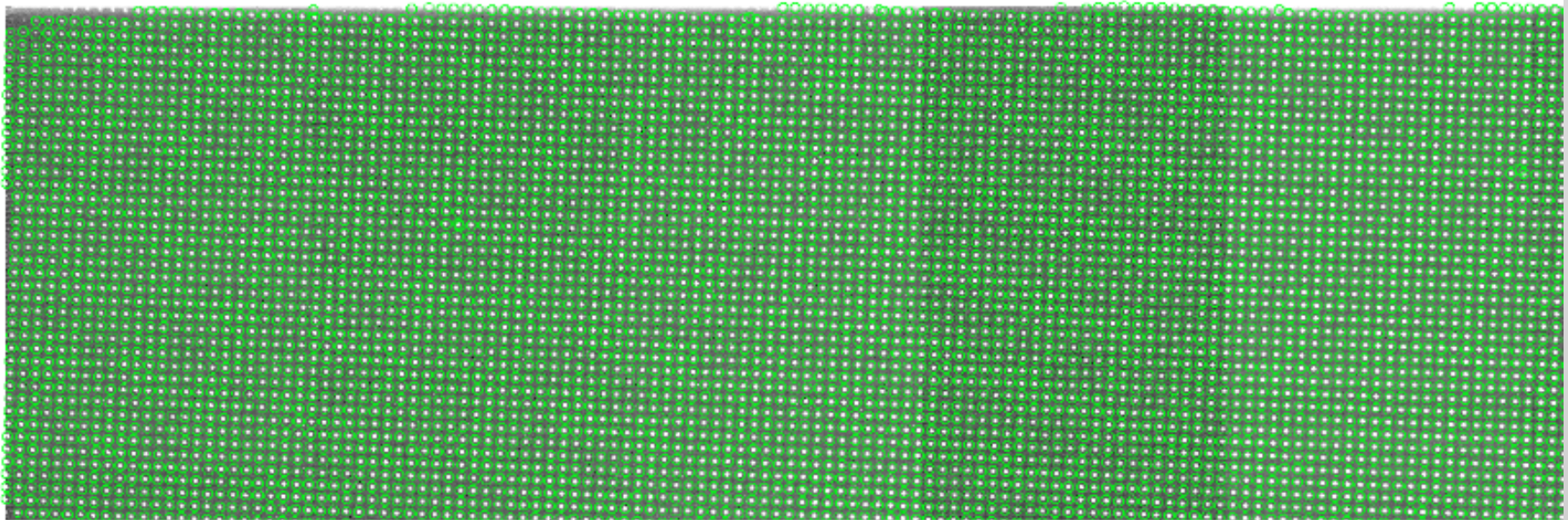
- XYZ pos.  $\sim 1\mu\text{m}$
- flux of light to 1%
- filter, integration time, backside bias, etc.

Use this as a pixel  
modeler





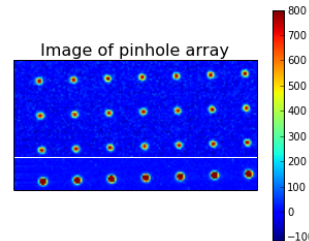
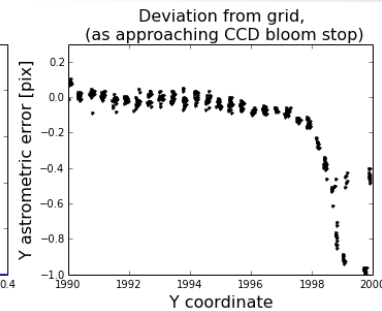
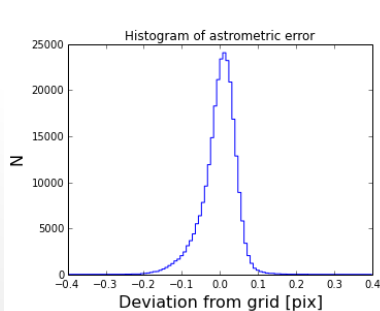
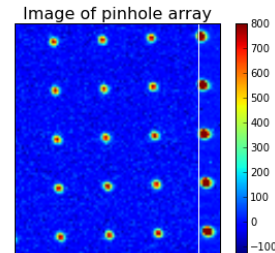
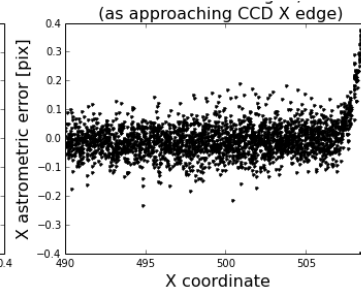
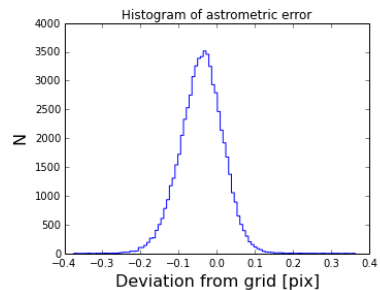
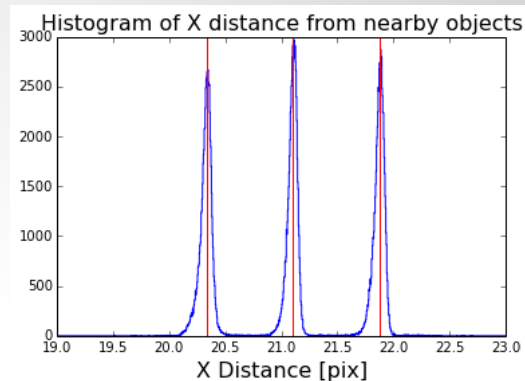
**40,000 pinholes per exposure x hundreds of exposures=  
millions of data points in one run**



# edge effects

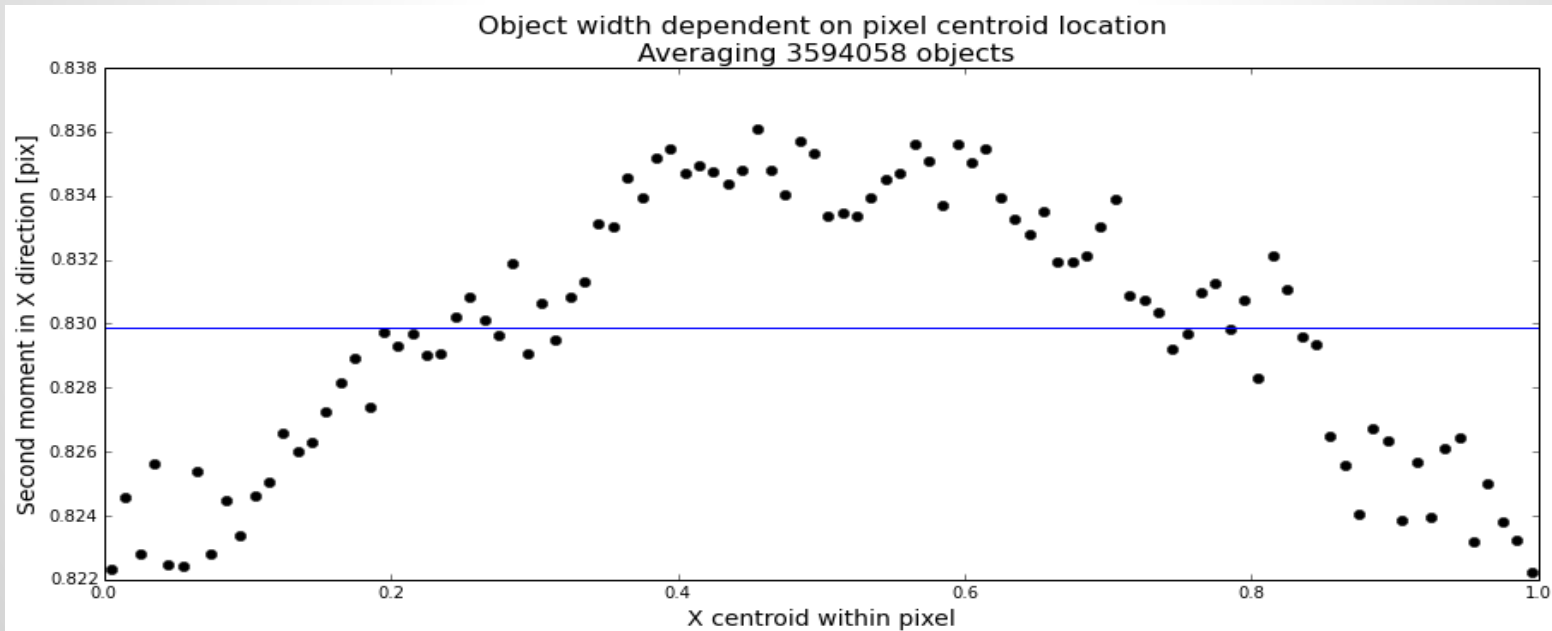
- use pinhole grid in each image to define local coordinate system independent of CCD, calculate “astrometric residual”
  - deviation from local astrometric system at edges
- Other methods...

subpixel precision on local astrometry



# pixel centroid effect

- used sextractor centroids and widths to test if width is dependent upon location within pixel
  - model error or physics within pixel?



**questions, comments, ideas?**